13.3. Transformer Networks

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Vaswani et al. (2017) proposed to go one step further: instead of using attention mechanisms as a supplement to standard convolutional and recurrent operations, they designed a models combining only attention layers.

They designed this “transformer” for a sequence-to-sequence translation task, but it is currently key to state-of-the-art approaches across NLP tasks.
They first introduce a multi-head attention module.

\[
\text{Attention}(Q, K, V) = \text{softmax} \left( \frac{Q K^\top}{\sqrt{d_k}} \right) V
\]

\[
\text{MultiHead}(Q, K, V) = \text{Concat} (H_1, \ldots, H_h) W^O
\]

with

\[
H_i = \text{Attention} \left( Q W_i^Q, K W_i^K, V W_i^V \right), \ i = 1, \ldots, h
\]

\[
W_i^Q \in \mathbb{R}^{d_{\text{model}} \times d_k}, \ W_i^K \in \mathbb{R}^{d_{\text{model}} \times d_k}, \ W_i^V \in \mathbb{R}^{d_{\text{model}} \times d_v}, \ W^O \in \mathbb{R}^{hd_v \times d_{\text{model}}}
\]
Their complete model is composed of:

- An encoder that combines $N = 6$ modules each composed of a multi-head attention sub-module, and a [per-component] one hidden-layer MLP, with residual pass-through and layer normalization.
- A decoder with a similar structure, but with causal attention layers to allow for regression training, and additional attention layers that attend to the layers of the encoder.
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Positional information is provided through an additive positional encoding of same dimension $d_{model}$ as the internal representation, and is of the form

$$PE_{t,2i} = \sin \left( \frac{t}{10,000 \frac{2i}{d_{model}}} \right)$$

$$PE_{t,2i+1} = \cos \left( \frac{t}{10,000 \frac{2i+1}{d_{model}}} \right).$$
3.1 Encoder and Decoder Stacks

Encoder: The encoder is composed of a stack of $N = 6$ identical layers. Each layer has two sub-layers. The first is a multi-head self-attention mechanism, and the second is a simple, position-wise fully connected feed-forward network. We employ a residual connection [11] around each of the two sub-layers, followed by layer normalization [1]. That is, the output of each sub-layer is $\text{LayerNorm}(x + \text{Sublayer}(x))$, where $\text{Sublayer}(x)$ is the function implemented by the sub-layer itself. To facilitate these residual connections, all sub-layers in the model, as well as the embedding layers, produce outputs of dimension $d_{\text{model}} = 512$.

Decoder: The decoder is also composed of a stack of $N = 6$ identical layers. In addition to the two sub-layers in each encoder layer, the decoder inserts a third sub-layer, which performs multi-head attention over the output of the encoder stack. Similar to the encoder, we employ residual connections around each of the sub-layers, followed by layer normalization. We also modify the self-attention sub-layer in the decoder stack to prevent positions from attending to subsequent positions. This masking, combined with the fact that the output embeddings are offset by one position, ensures that the predictions for position $i$ can depend only on the known outputs at positions less than $i$.

3.2 Attention

An attention function can be described as mapping a query and a set of key-value pairs to an output, where the query, keys, values, and output are all vectors. The output is computed as a weighted sum of the values, where the weight assigned to each value is computed by a compatibility function of the query with the corresponding key.

(Vaswani et al., 2017)
The architecture is tested on English-to-German and English-to-French translation using the standard WMT2014 datasets.

- English-to-German: 4.5M sentence pairs, 37k tokens vocabulary.
- English-to-French: 36M sentence pairs, 32k tokens vocabulary.
- 8 P100 GPUs (150 TFlops FP16), 0.5 day for the small model, 3.5 days for the large one.
Table 2: The Transformer achieves better BLEU scores than previous state-of-the-art models on the English-to-German and English-to-French newstest2014 tests at a fraction of the training cost.

<table>
<thead>
<tr>
<th>Model</th>
<th>BLEU</th>
<th>Training Cost (FLOPs)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>EN-DE</td>
<td>EN-FR</td>
</tr>
<tr>
<td></td>
<td>EN-DE</td>
<td>EN-FR</td>
</tr>
<tr>
<td>ByteNet [18]</td>
<td>23.75</td>
<td></td>
</tr>
<tr>
<td>Deep-Att + PosUnk [39]</td>
<td>24.6</td>
<td>2.3 · 10^{19}</td>
</tr>
<tr>
<td>GNMT + RL [38]</td>
<td>25.16</td>
<td>9.6 · 10^{18}</td>
</tr>
<tr>
<td>ConvS2S [9]</td>
<td>26.03</td>
<td>2.0 · 10^{19}</td>
</tr>
<tr>
<td>MoE [32]</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Deep-Att + PosUnk Ensemble [39]</td>
<td>26.30</td>
<td>1.8 · 10^{20}</td>
</tr>
<tr>
<td>GNMT + RL Ensemble [38]</td>
<td>26.36</td>
<td>7.7 · 10^{19}</td>
</tr>
<tr>
<td>ConvS2S Ensemble [9]</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Transformer (base model)</td>
<td>27.3</td>
<td>3.3 · 10^{18}</td>
</tr>
<tr>
<td>Transformer (big)</td>
<td>28.4</td>
<td>2.3 · 10^{19}</td>
</tr>
</tbody>
</table>

(Vaswani et al., 2017)
The Law will never be perfect, but its application should be just—this is what we are missing, in my opinion.

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(Vaswani et al., 2017)
The Universal Transformer (Dehghani et al., 2018) is a similar model where all the blocks are identical, resulting in a recurrent model that iterates over consecutive revisions of the representation instead of positions.

Additionally the number of steps is modulated per position dynamically.
Transformer self-training and fine-tuning for NLP
The transformer networks were introduced for translation, and trained with a supervised procedure, from pairs of sentences.

However, as for word embeddings, they can be trained in an unsupervised manner, for auto-regression or as denoising auto-encoders, from very large data-sets, and fine-tuned on supervised tasks with small data-sets.
Figure 3: Differences in pre-training model architectures. BERT uses a bidirectional Transformer. OpenAI GPT uses a left-to-right Transformer. ELMo uses the concatenation of independently trained left-to-right and right-to-left LSTMs to generate features for downstream tasks. Among the three, only BERT representations are jointly conditioned on both left and right context in all layers. In addition to the architecture differences, BERT and OpenAI GPT are fine-tuning approaches, while ELMo is a feature-based approach.

(Devlin et al., 2018)
GPT (Generative Pre-Training, Radford, 2018) is a transformer trained for auto-regressive text generation.
“GPT-2 is a large transformer-based language model with 1.5 billion parameters, trained on a dataset of 8 million web pages. GPT-2 is trained with a simple objective: predict the next word, given all of the previous words within some text. The diversity of the dataset causes this simple goal to contain naturally occurring demonstrations of many tasks across diverse domains. GPT-2 is a direct scale-up of GPT, with more than 10X the parameters and trained on more than 10X the amount of data.”

(Radford et al., 2019)
We can install implementations of the various flavors of transformers from HuggingFace (https://huggingface.co/)

```
pip install transformers
```

and use pre-trained models as we did for vision.
import torch

from transformers import GPT2Tokenizer, GPT2LMHeadModel

tokenizer = GPT2Tokenizer.from_pretrained('gpt2')
model = GPT2LMHeadModel.from_pretrained('gpt2')
model.eval()

tokens = tokenizer.encode('Studying Deep-Learning is')

for k in range(11):
    outputs, _ = model(torch.tensor([tokens]))
    next_token = torch.argmax(outputs[0, -1])
    tokens.append(next_token)

print(tokenizer.decode(tokens))

prints

Studying Deep-Learning is a great way to learn about the world around you.
BERT (Bidirectional Encoder Representation from Transformers, Devlin et al., 2018) is a transformer pre-trained with:

- Masked Language Model (MLM), that consists in predicting [15% of] words which have been replaced with a “MASK” token.
- Next Sentence Prediction (NSP), which consists in predicting if a certain sentence follows the current one.

It is then fine-tuned on multiple NLP tasks.
Figure 1: Overall pre-training and fine-tuning procedures for BERT. Apart from output layers, the same architectures are used in both pre-training and fine-tuning. The same pre-trained model parameters are used to initialize models for different downstream tasks. During fine-tuning, all parameters are fine-tuned. `[CLS]` is a special symbol added in front of every input example, and `[SEP]` is a special separator token (e.g., separating questions/answers).

(Devlin et al., 2018)
BERT

(a) Sentence Pair Classification Tasks:
MNLI, QQP, QNLI, STS-B, MRPC, RTE, SWAG

Start/End Span

(c) Question Answering Tasks:
SQuAD v1.1

(b) Single Sentence Classification Tasks:
SST-2, CoLA

(d) Single Sentence Tagging Tasks:
CoNLL-2003 NER

(Devlin et al., 2018)
Prepositions attend to their objects - 76.3% accuracy at the pobj relation.

Noun modifiers (e.g., determiners) attend to their noun - 94.3% accuracy at the det relation.

Passive auxiliary verbs attend to the verb they modify - 82.5% accuracy at the auxpass relation.

Possessive pronouns and apostrophes attend to the head of the corresponding NP - 80.5% accuracy at the poss relation.

Coreferent mentions attend to their antecedents - 65.1% accuracy at linking the head of a coreferent mention to the head of an antecedent.

Figure 5: BERT attention heads that correspond to linguistic phenomena. In the example attention maps, the darkness of a line indicates the strength of the attention weight. All attention to/from red words is colored red; these colors are there to highlight certain parts of the attention heads’ behaviors. For Head 9-6, we don’t show attention to [SEP] for clarity. Despite not being explicitly trained on these tasks, BERT’s attention heads perform remarkably well, illustrating how syntax-sensitive behavior can emerge from self-supervised training alone.

(Clark et al., 2019)
**Head 7-6**

- **Possessive pronouns** and apostrophes attend to the head of the corresponding NP
- 80.5% accuracy at the `poss` relation

**Head 9-6**
- Prepositions attend to their objects
- 76.3% accuracy at the `pobj` relation

**Head 8-11**
- Noun modifiers (e.g., determiners) attend to their noun
- 94.3% accuracy at the `det` relation

**Head 8-10**
- Direct objects attend to their verbs
- 86.8% accuracy at the `dobj` relation

**Head 5-4**
- Coreferent mentions attend to their antecedents
- 65.1% accuracy at linking the head of a coreferent mention to the head of an antecedent

**Head 4-10**
- **Passive auxiliary verbs** attend to the verb they modify
- 82.5% accuracy at the `auxpass` relation

**Head 10-8**
- Possessive pronouns and apostrophes attend to the head of the corresponding NP
- 80.5% accuracy at the `poss` relation

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Head 9-6
- Prepositions attend to their objects
- 76.3% accuracy at the pobj relation

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- Coreferent mentions attend to their antecedents
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(Clark et al., 2019)
Attention in computer vision
Wang et al. (2018) proposed an attention mechanism for images, following the model from Vaswani et al. (2017).

\[ y = \text{softmax} \left( (W_\theta x)^\top (W_\phi x) \right) W_g x. \]
They insert “non-local blocks” in residual architectures and get improvements on both video and images classification.

Figure 2. A spacetime non-local block. The feature maps are shown as the shape of their tensors, e.g., $T \times H \times W \times 1024$ for 1024 channels (proper reshaping is performed when noted). “$\otimes$” denotes matrix multiplication, and “$\oplus$” denotes element-wise sum. The softmax operation is performed on each row. The blue boxes denote $1 \times 1 \times 1$ convolutions. Here we show the embedded Gaussian version, with a bottleneck of 512 channels. The vanilla Gaussian version can be done by removing $\theta$ and $\phi$, and the dot-product version can be done by replacing softmax with scaling by $1/N$.

(Wang et al., 2018)
Figure 3. Examples of the behavior of a non-local block in res3 computed by a 5-block non-local model trained on Kinetics. These examples are from held-out validation videos. The starting point of arrows represents one $x_i$, and the ending points represent $x_j$. The 20 highest weighted arrows for each $x_i$ are visualized. The 4 frames are from a 32-frame input, shown with a stride of 8 frames. These visualizations show how the model finds related clues to support its prediction.

(Wang et al., 2018)
Ramachandran et al. (2019) replaced convolutions with local attention.

\[
y_{i,j} = \sum_{(a,b) \in \mathcal{N}(i,j)} W_{i-a,j-b} x_{a,b} \quad \text{(Convolution)}
\]

\[
y_{i,j} = \sum_{(a,b) \in \mathcal{N}(i,j)} \text{softmax}_{a,b} \left( (W_Q x_{i,j})^\top (W_K x_{a,b}) \right) v_{a,b} \quad \text{(Local attention)}
\]

Figure 2: An example of a $3 \times 3$ convolution. The output is the inner product between the local window and the learned weights.

Figure 3: An example of a local attention layer over spatial extent of $k = 3$.

(Ramachandran et al., 2019)
Table 1: ImageNet classification results for a ResNet network with different depths.

<table>
<thead>
<tr>
<th>Model</th>
<th>FLOPS (B)</th>
<th>Params (M)</th>
<th>Acc. (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Baseline</td>
<td>4.7</td>
<td>13.7</td>
<td>74.5</td>
</tr>
<tr>
<td>Conv-stem + Attention</td>
<td>4.5</td>
<td>10.3</td>
<td>75.8</td>
</tr>
<tr>
<td>Full Attention</td>
<td>4.7</td>
<td>10.3</td>
<td>74.8</td>
</tr>
</tbody>
</table>

Figure 5: Comparing parameters and FLOPS against accuracy on ImageNet classification across a range of network widths for ResNet-50. Attention models have fewer parameters and FLOPS while improving upon the accuracy of the baseline.

(Ramachandran et al., 2019)
“A fully attentional network based off of the proposed stand-alone local self-attention layer achieves competitive predictive performance on ImageNet classification and COCO object detection tasks while requiring fewer parameters and floating point operations than the corresponding convolution baselines.”

(Ramachandran et al., 2019)
Cordonnier et al. (2020) showed that provided with proper positional encoding multi-head multiplicative attention layers can encode convolutions with filter support of size the number of heads:

“A multi head self-attention layer with $N_h$ heads of dimension $D_h$, output dimension $D_{out}$ and a relative positional encoding of dimension $D_p \geq 3$ can express any convolutional layer of kernel size $\sqrt{N_h} \times \sqrt{N_h}$ and $\min (D_h, D_{out})$ output channels.”

(Cordonnier et al., 2020)
Figure 5: Attention probabilities of each head (column) at each layer (row) using learned relative positional encoding without content-based attention. The central black square is the query pixel. We reordered the heads for visualization and zoomed on the 7x7 pixels around the query pixel.

Figure 6: Attention probabilities for a model with 6 layers (rows) and 9 heads (columns) using learned relative positional encoding and content-content based attention. Attention maps are averaged over 100 test images to display head behavior and remove the dependence on the input content. The black square is the query pixel. More examples are presented in Appendix A.

(Cordonnier et al., 2020)
https://epfml.github.io/attention-cnn/
The end
References


